

MATHEMATICS QUIZ

Dr T.Rajaretnam

St.Joseph's College(Autonomous)

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1 Round 3

■ Questions

Choose the Correct Answer

If $(\sin \theta + \operatorname{cosec} \theta) = 2$ then $\sin^2 \theta + \operatorname{cosec}^2 \theta$ is equal to

- (a) 1
- (b) 4
- (c) 2
- (d) 0



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[▶ goto exp](#)

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$\sqrt{2 + \sqrt{2 + 2 \cos 4\theta}}$ is equal to

- (a) $\cos \theta$
- (b) $\cos 2\theta$
- (c) $2 \cos \theta$
- (d) $2 \cos 2\theta$

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If a triangle ABC , right angled at C ,then

$\tan A + \tan B$ is equal to

- (a) $a + b$
- (b) $\left(\frac{c^2}{ab}\right)$
- (c) $\left(\frac{a^2}{bc}\right)$
- (d) $\left(\frac{b^2}{ac}\right)$

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Choose the Correct Answer

The area between the curves $y^2 = x$, $x^2 = y$ is equal to

(a) $\frac{16}{3}$

(b) 1

(c) $\frac{1}{4}$

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The angle between the pair of straight

lines $y^2 \sin^2 \theta - xy \sin^2 \theta + x^2(\cos^2 \theta - 1) = 0$ is

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(b) $\frac{\pi}{4}$

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The eccentricity of the conic represented by

$$x^2 - y^2 - 4x + 4y + 16 = 0 \text{ is}$$

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- (b) 1
- (c) 2
- (d) $\frac{1}{2}$



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▶ Return

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▶ Return

Answer



Answer

$$2 + 2 \cos 4\theta = 2(1 + \cos 4\theta)$$



Answer

$$\begin{aligned}2 + 2 \cos 4\theta &= 2(1 + \cos 4\theta) \\ &= 2 \cdot 2 \cos^2 2\theta\end{aligned}$$



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$$\therefore \sqrt{2 + \sqrt{2 + 2 \cos 4\theta}} = \sqrt{2 + 2 \cos 2\theta}$$



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▶ Return



Answer

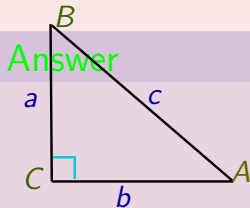
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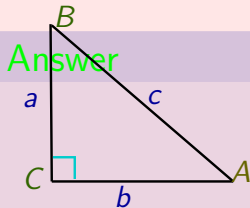
▶ Return



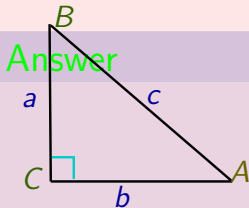
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$$\tan A = \frac{a}{b} , \tan B = \frac{b}{a}$$

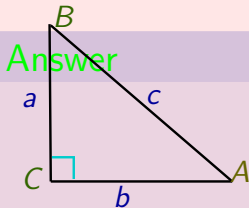


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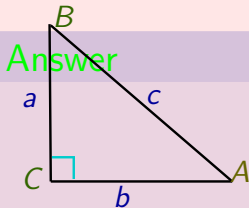
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▶ Return

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$$\therefore \text{here area} = \frac{1 \times 1}{3}$$

▶ Return

Answer



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$$ax^2 + 2hxy + by^2 = 0$$



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If $a + b = 0$ then the two lines are perpendicular

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$$a + b = \sin^2 \theta + (\cos^2 \theta - 1) = 1 - 1 = 0$$

$$\therefore \theta = \frac{\pi}{2}$$

▶ Return



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$$\therefore e = \sqrt{2}$$

▶ Return